

**Errata et Addenda to the First Printing of the Book**  
**Advanced Topics in Computational Number Theory**  
 by **Henri Cohen**  
 (20000615 Version)

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- p. 23 line 8, instead of “Corollary 1.2.11” read “Corollary 1.3.9”
- p. 31 line -11, instead of “ $\mathbf{c}_j = \mathfrak{g}_{n+1-j} \mathfrak{g}_{n-j}^{-1}$ ” read “ $\mathbf{c}_j = \mathfrak{g}_j \mathfrak{g}_{j+1}^{-1}$ ”
- p. 31 line -7, instead of “ $\mathfrak{g}_j(A) = \mathbf{c}_{n+1-j} \cdots \mathbf{c}_n$ ” read “ $\mathfrak{g}_j(A) = \mathbf{c}_j \cdots \mathbf{c}_n$ ”
- p. 44 line 3 of step 4 of Algorithm 1.7.3, exchange “ $a_{i,j}$ ” with “ $a_{i,i}$ ” (twice)
- p. 44 line 3 of step 7 of Algorithm 1.7.3, instead of “ $a_{j,i}A'_j - A'_i$ ” read “ $A'_j - a_{j,i}A'_i$ ” and instead of “ $a_{j,i}V'_j - V'_i$ ” read “ $V'_j - a_{j,i}V'_i$ ”
- p. 45 line 13, instead of “ $\mathbf{c} = \sum_i \mathbf{a}'_i \mathbf{b}'_i$ ” read “ $\mathbf{c} = \sum_i \mathbf{a}'_i \mathbf{b}'_i{}^{-1}$ ”
- p. 45 line 17, instead of “ $(n-i) \times (n-i)$ ” read “ $(n+1-i) \times (n+1-i)$ ”
- p. 45 line -7, instead of “step 5” read “step 2”
- p. 46 line 3 of Exercise 1, exchange “ $1/|\mathcal{N}(x)|$ ” and “ $|\mathcal{N}(x)|$ ”
- p. 60 line 10, instead of “ $\theta_1 = -R'(X)/R'_Z(X, k)$ ” read “ $\theta_1 = -R'_Z(X, k)/R'(X)$ ”
- p. 60 line 15, instead of “ $\theta_1^i \theta_2^j$ ” read “ $\theta_1^{i_1} \theta_2^{i_2}$ ”
- p. 62 line -5 and line -4, instead of “ $L_1(X)$ ” read “ $L_1[X]$ ”
- p. 65 line -8, instead of “ $\sum_{0 \leq j < n_1} c_{i,j} a_j = b_i$ ” read “ $\sum_{0 \leq j < n_1} c_{i,j} b_j = a_i$ ”
- p. 65 line -3 (twice) and line -1 (once), instead of “ $\alpha$ ” read “ $\theta_2$ ”
- p. 66 line 3 of step 2 of Algorithm 2.1.12, instead of “ $(1, 0, \dots, 0)^t$ ” read “ $(0, 1, 0, \dots, 0)^t$ ”
- p. 85 line 8, instead of “ $\alpha_j$ ” read “ $\gamma_j$ ”
- p. 88 line 1 of Lemma 2.3.7, instead of “ $\alpha \in K$ ” read “ $\alpha \in L$ ”
- p. 88 line -12, instead of “ $\mathcal{N}_{L/K}(I) \in I$ ” read “ $\mathcal{N}_{L/K}(I) \subset I$ ”
- p. 92 lines 8 and 9, exchange “ $\mathfrak{P}$  is unramified” with “ $\mathfrak{P}$  is ramified”
- p. 99 Replace steps 3 and 4 of Algorithm 2.3.21 by the following:
- 3. [Terminate] Using Algorithm 1.5.1, compute an HNF pseudo-basis  $(\gamma_i, \mathbf{c}_i)$  for the intersection  $I^{-1} \leftarrow I_1 \cap I_2$ .
- p. 106 line -1, instead of “ $\mathbb{Z}_K \setminus \mathfrak{p}^{-1}$ ” read “ $\mathfrak{p}^{-1} \setminus \mathbb{Z}_K$ ”
- p. 110 lines 5 and 6 of Algorithm 2.4.12, replace twice “ $\sum_{1 \leq k \leq n}$ ” by “ $\sum_{0 \leq k \leq n}$ ”
- p. 114 line 19, instead of “ $\theta \in K$ ” read “ $\theta_1 \in K$ ”
- p. 131 Exercise 33, instead of “proof given in” read “proof of”
- p. 131 Exercise 34, replace twice “ $t_i$ ” by “ $T_i$ ”, and replace four times “ $r_i$ ” by “ $R_i$ ”
- p. 131 Exercise 36, instead of “ $\omega^2(\omega + 3)$ ” read “ $\omega^2(-\omega - 3)$ ”
- p. 135 line -5, instead of “ $\rho(\alpha) = (\overline{\alpha}, (\text{sign}(\sigma_i(\alpha))_{\sigma_i \in \mathfrak{m}_\infty}))$ ” read “ $\rho(\alpha) = (\overline{\alpha}, (\text{sign}(\sigma_i(\alpha)))_{\sigma_i \in \mathfrak{m}_\infty})$ ”
- p. 161 Exercise 7 d), instead of “necessary” read “necessarily”
- p. 161 Exercise 15 a), add the property “ $\mathfrak{d}(L/K) \mid \mathfrak{m}_0^{\ell^r - 1}$ ”
- p. 187 line 1, instead of “ $\phi(\beta) = \overline{\beta}$ , and” read “ $\phi(\beta) = \overline{\beta}$ , and”

- p. 201 line 3 of step 2 of Algorithm 4.2.16, instead of " $\beta \leftarrow \beta \prod_i (1 + \gamma_{a,i}^{-y_{a,i}})$ " read " $\beta \leftarrow \beta \prod_i (1 + \gamma_{a,i})^{-y_{a,i}}$ "
- p. 212 line -14, instead of " $(\mathbb{Z}/\mathfrak{m})^*$ " read " $(\mathbb{Z}_K/\mathfrak{m})^*$ "
- p. 221 Exercise 18 c), instead of "prime ideal below" read "prime number below"
- p. 226 line 9, instead of "field  $K$ , a congruence" read "field  $K$  and a congruence"
- p. 230 middle, instead of "the next section" read "Section 5.2.4"
- p. 255 line -3, instead of " $\gamma \in K^{*\ell}$ " read " $\gamma \in K^*$ "
- p. 260 line -10, instead of "Thus," read "Hence,"
- p. 293 Exercise 4 a), instead of "exists" read "exist" (twice)
- p. 308 line 3, instead of " $(-i)^{f_\infty}$ " read " $(-i)^{|f_\infty|}$ "
- p. 308 step 5 of Algorithm 6.2.4, instead of " $(-i)^{|f_\infty|}$ " read " $(-i)^{|f_\infty|}$ "
- p. 315 middle, instead of "elliptic function  $j(\tau)$ " read "modular function  $j(\tau)$ "
- p. 318 middle, instead of " $\left(\frac{2i\pi}{\omega_2}\right)^{24}$ " read " $\left(\frac{2i\pi}{\omega_2}\right)^{12}$ "
- p. 345 Remove Exercise 8 (it is Exercise 15 d)
- p. 346 Exercise 25, put the parenthetical statement "(where as usual we set  $\mathfrak{f} \cap \mathbb{Z} = f\mathbb{Z}$ )" at the end of the sentence, without parentheses
- p. 425 line 2 of step 9, instead of " $d_3 \leftarrow \lceil (b-s)/2 \rceil - 1$ ,  $d_4 \leftarrow \lfloor (b+s)/2 \rfloor + 1$ " read " $d_3 \leftarrow \lceil (b-s)/2 \rceil$ ,  $d_4 \leftarrow \lfloor (b+s)/2 \rfloor$ "
- p. 434 line 11, instead of " $\alpha/\alpha'$ " read " $(\alpha/\alpha')\mathbb{Z}_K$ "
- p. 434 line -13, instead of "whose prime factors are only prime ideals above 2" read "dividing 2"
- p. 439 line 2 of (4), instead of "they will" read "it will"
- p. 439 line 5 of (4), instead of "repeat" read "recompute"
- p. 439 middle, instead of "the case of prime degree" read "the prime degree case"
- p. 444 line -8, instead of " $G_{18}^+$ ,  $G_{18}^-$ ,  $G_{36}$ , and  $G_{72}$ " read " $G_{36}^+$ ,  $G_{36}^-$ , and  $G_{72}$ "
- p. 451 line -3, instead of "Schwartz's" read "Cauchy-Schwarz's"
- p. 455 line 1, instead of "Schwartz's" read "Cauchy-Schwarz's"
- p. 469 replace Exercise 6 b) by the following: "Let  $R_1$  denote an even integer such that  $0 \leq R_1 \leq 2r_1$ . Show that the number of  $K$ -isomorphism classes of quadratic extensions  $L/K$  with  $\mathcal{N}_{K/\mathbb{Q}}(\mathfrak{d}(L/K)) \leq x$  and  $R_1$  real embeddings is asymptotic to  $((\binom{r_1}{R_1/2})/2^{r_1})Q_K \cdot x$ , where  $Q_K$  is as above."
- p. 470 line 1 of Exercise 14, replace "and" by ",",
- p. 471 Exercise 16 a), instead of "Schwartz's" read "Cauchy-Schwarz's"
- p. 471 Exercise 16 a), instead of "show that" read "prove *Lagrange's identity*"
- p. 483 line -6, instead of " $\theta_k(\tau)(\theta_0(\sigma)^k - 1) = 0$ " read " $(\theta_0(\sigma)^k - 1)\theta_k(\tau) = 0$ "
- p. 484 line -12, instead of " $\mathfrak{D}(L/K) = \mathbb{Z}_L^*$ " read " $\mathbb{Z}_L^* = \mathfrak{D}(L/K)^{-1}$ "
- p. 488 middle, instead of " $v_{\mathfrak{p}}(\mathfrak{f}_2)$  is even" read " $v_{\mathfrak{p}}(\mathfrak{f}_2)$  is even when  $\mathfrak{p}$  is ramified in  $K_2/K$ "
- p. 520 rewrite Exercise 12 as follows: "Let  $L/K$  be an extension of number fields, let  $P$  be a monic polynomial with coefficients in  $K$ , let  $\mathfrak{p}$  be a prime ideal of  $K$ , and let  $\alpha \in L$  be a root of  $P$ . Assume that the  $\mathfrak{p}$ -adic valuations of all the coefficients of  $P$  are nonnegative. Show that  $v_{\mathfrak{p}}(\alpha) \geq 0$  for any prime ideal  $\mathfrak{P}$  of  $L$  above  $\mathfrak{p}$ ."

p. 520 line 1 of Exercise 15, instead of “let  $\ell$  is a prime number” read “ $\ell$  a prime number”

p. 558 add at the appropriate place “ $\Gamma_\infty$ : group of integer translations, 122”

p. 573 add at the appropriate place “Lagrange’s identity, 471”